



**Original Article**

## **Comparison of Published and Proposed Models for Estimation of Soil Erodibility in a Semiarid Region**

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### **ABSTRACT**

As the in-situ determination of the soil erodibility factor is in need of elaborate setting up and observation for lengthy periods of time, the use of pedotransfer functions is a good alternative for measurement at a large scale and is highly suitable for soil mapping. Therefore, a study was initiated to select the best model or index for estimating soil erodibility (K) based on soil properties under different land uses over the southern and middle parts of Erbil province. To achieve this goal, soil samples were obtained from the top 0.2 m at 30 locations within the study area. The most commonly used models and a proposed model were compared and ranked based on their power of predictability. The results indicated that 67% of the estimated soil erodibility by the reference method fell in the moderate and fairly high classes. It is also apparent from the displayed results that more than 73% of sampling sites have a dispersion ratio of more than 15% thereby indicating that the majority of the soils are highly vulnerable to erosion. Among soil erodibility indices, only Critical Level of Organic Matter (CLOM) exhibits the strongest correlation with K ( $r = 0.01$ ). It was also observed that the truncated Wischmeier and Smith model has the highest predictability power for estimating K, followed by the proposed multiple linear models, while the Shirazi model exhibited the poorest performance. Further, the soil erodibility estimated by K6 and K2 exhibited better harmony with land use variation than that of the remaining models. It was also noticed that K gained the highest value at the north and tends to decrease from north to south.

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**Keywords:** Soil erodibility, Model evaluation, Model building, Erodibility indices, Indirect estimation.

### **1 Introduction**

Overexploitation of natural resources and conventional agricultural practices without conservation practices has led to severe soil erosion. Therefore, estimation of soil erosion has always been a key concern for soil conservation specialists and ecologists [1]. The acceleration of erosion as a natural process has become a big challenge as it gives rise to intensive land deterioration, environmental disturbance, and disorder of the socio-economic condition of the inhabitants [2,3]. Soil erosion measurement is a frustrating process on account of logistics and longer data series requirements. This is especially true in underdeveloped countries, with longer and the frequent data collection. The problems become more complicated in developing countries due to resource constraints [4]. Soil erodibility (K-factor) in the universal soil loss equation can be

computed by the ratio of soil loss per unit rainfall erosivity and per unit area from a standard plot [5].

Soil erodibility is one of the vital parameters of erosion predicting models [6]. The measurement of this parameter is tedious and time-consuming in the field due to the vast cost of field setup and the time dedicated to frequent measurements. Accordingly, field measurements of the K-factor have been performed for limited reference soils [7]. Direct measurements of erodibility have been made on only a few benchmark soils. To find a remedy for this situation, Wischmeier and Mannering [8] originally proposed an erodibility model based on 15 soil properties and the interactions among them. Later on, soil properties were shrunk to only four properties, which were soil separates, soil organic content, soil structure, and permeability.

Because of many constraints and substantial uncertainties in in-situ measurement of K-factors, numerous empirical models have been suggested for indirect estimation of this parameter. For instance, Wischmeier & Smith [5] developed a model for indirect estimation of soil erodibility based on soil texture, organic

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content, structure, and permeability as input variables. Renard et al. <sup>[9]</sup> related soil erodibility to the mean geometric particle diameter of different textural classes and indicated that such models are useful for sites with limited data, especially when there is no gathered data on soil structure, soil permeability, soil organic content, and very fine sand. Also, Denardin <sup>[10]</sup> developed a regression model with M (the sum of silt and very fine sand multiplied by  $(100 - \text{clay})$ ), structure code, the mean weighted diameter of particles less than 2 mm, and the ratio of soil organic content to the ratio of particles sandwiched between 1 and 2 mm. Furthermore, Sharpley and Williams <sup>[11]</sup> derived a model in the form of the product of four functions (A, B, C, and D).

Bonilla and Johnson <sup>[12]</sup> revealed that indirect methods can be employed to determine this factor and make such studies possible. Adhikary et al. <sup>[13]</sup> observed that the erodibility model that uses soil texture (particle size) and organic content exhibited better harmony with land use variation than erodibility models that depend only on soil separates. On the other hand, Anache et al. <sup>[14]</sup> revealed that soil properties such as texture, structure, organic content, and its chemical composition are significantly correlated with the susceptibility of soil to erosion. Based on these properties, a host of indices were also developed. These indices are a beneficial substitute for planning suitable treatment procedures in areas where the generation of soil erosion is a constraint. Among the most widely used indices are clay ratio, dispersion ratio, suspension ratio, ratio of clay content to moisture equivalent, etc. <sup>[15]</sup>. Chorley <sup>[16]</sup> developed an erodibility index based on a combination of permeability and shear resistance, while Wischmeier and Smith <sup>[17]</sup> suggested the K-factor depending on soil properties influencing dispersion and water transmission. The erosion index was also derived as an erodibility index based on Indian investigations <sup>[18]</sup>. The dispersion ratio value can be used as a good indicator for the vulnerability of soils to erosion <sup>[19]</sup>. The cutoff value of 15% for dispersion ratio can be considered as the cutoff value between erosive and non-erosive soils <sup>[20]</sup>. Remote Sensing accompanied with GIS is one of the powerful ways of soil mapping at different spatial and temporal resolutions <sup>[21]</sup>.

Erodibility indices can support in diagnosing zones that are vulnerable to erosion, and protective measures can be planned accordingly. Furthermore, the models that are derived for a reference area are coherent with the soil features of that area, but they may not agree well with the features of the area under investigation. Therefore, the current study was initiated to target the following objectives: 1) To select the best soil erodibility index that is closely related to the susceptibility of soils to erosion over the study area; 2) to test the performance of the previously

published and two proposed models for assessing soil erodibility, 3) to build a model for predicting soil erodability across the study area, and 4) to generate continuous surfaces for soil erodibility over the study area.

## 2 Materials and Methods

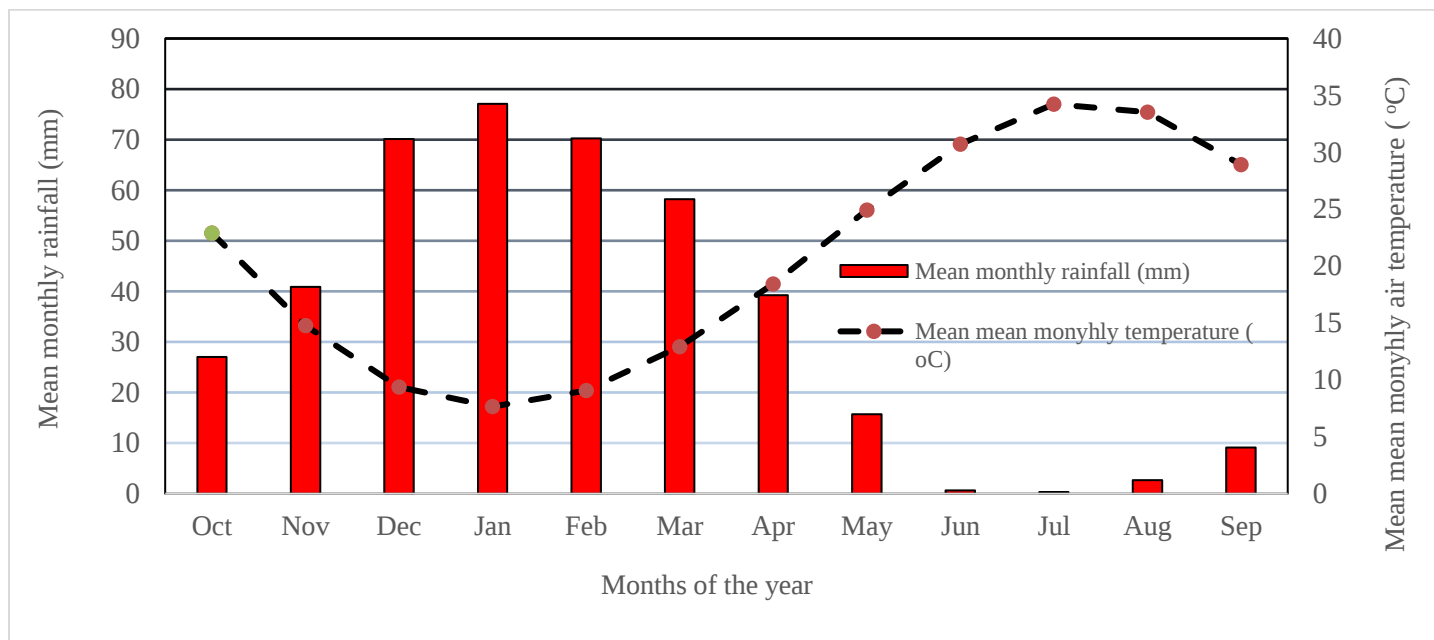
### 2.1 Description of the Study Area

The study area occupies nearly the southern and middle parts of Erbil Governorate. It spans a total area of approximately 9000 km<sup>2</sup> and covers several watersheds with different land uses. Geographically, it is situated between latitudes of 35.5000° N and 36.700° N and longitudes of 43.171° E and 44.8333° E. The area feeds the Greater Zab and the Lesser Zab rivers. The main watersheds within this area are: Koya, Hiran, Harir, Shaqlawa, Bastora, Bnaslaw, Qushtapa, Dibaga, and Makhmur. The dominant land uses encompassed agricultural (70%), grazing land (17%), and forest (13%).

The annual rainfall ranges from as low as 200 mm at Makhmur to as high as 900 mm at Shaqlawa. It has a unimodal distribution, and more than 95 % of the rainfall occurs between October and April. Contrarily, there is a water deficit over the remaining months of the year. The warmest and coldest months of the year are July and January, respectively.

On the basis of the classification scheme proposed by Koppen, the middle part of Erbil province (study area) is classified as temperate, dry summer, hot summer (CS<sub>a</sub>). While the area located in the southern part of the study area falls within the arid, steppe, hot (BS<sub>h</sub>). However, Figure 1 shows the distribution of mean monthly rainfall and mean monthly air temperature over the months of the year at Erbil Meteorological Station.

Vegetation is diverse, with no mountain vegetation can be found over most of its southern part, even the smaller woody shrublets have been removed by plough, fuel gatherer, and wood cutter. Patches of deciduous shrub trees and artificial spots can be observed over its upper part, forming open plant communities. The plain has a high potential for agricultural production. Dry farming is practiced to a high extent. Wheat farming accounts for the majority of arable lands, followed by barley, faba bean, chick pea, and maize. There are also scattered spots of irrigated lands, mostly along the existing streams. They are cropped with vegetables and orchards. Unlike the southern part, most areas within the low and high zones are except for the intermountain valleys, have steep to very steep slopes. Accordingly, they are utilized for grazing, forest lands, and marginal lands.



**Figure 1:** Distribution of mean monthly rainfall and mean monthly air temperature over the months of the year at Erbil meteorological station.

Tectonically, the southern parts are located within the foothill zone, while the areas surrounding the upper part are situated within the low folded zone. On the other hand, the mountainous area behind the upper part is located with high folded and thrust zones. Overall, the investigated area is underlain by various geological formations. The dominant rock formations encompass the Upper Bakhtiari, Lower Bakhtiari, Upper Fars, and Lower Fars.

Overall, the region can be considered as rough, broken, and stony lands. The mountains are mainly composed of limestone of different compositions. The existing soils have been either completely removed or so truncated that the diagnostic horizons of all orders other than Entisols are absent. The dominant soil groups than can be found over this area are: 1) Xerothents: a soil with a thin layer overlying stony or consolidated rocks, usually lime stone, 2) Rendolls: the soils with a dark brown or very dark brown to black granular surface layer of 15-20 cm in thickness overlying various kinds of limestone, 3) Chromoxererts: soils with a brown surface layer of about 20-40 cm grading into a lighter layer of lime accumulation [22]. Most of the existing soils at Erbil plain and the surrounding areas belong to Chromoxererts. This great group exists in the form of a deep profile, nearly free of rocks, medium potential to volume change, and has high agricultural potential. Additionally, there are scattered spots of red mud (Gercus formation), blue shales (Kolosh formation), and chalky soils (Shiranish formation) in the form of unconsolidated materials over steep slopes.

## 2.2 Sampling Strategy and Sampling Preparation

Prior to soil sampling, a field survey was made to estimate the level of soil erodibility and to postulate the soil characteristics. A Garmin portable GPS was employed to log the geospatial

information. A total of thirty representative soil samples were collected from the top 0.2 m of different locations covering different land uses over the study area during the late spring season of 2023 (Figure 2 and Table 1). The soil structure was described visually after dropping representative clods from a height of about 1 m in the field [23]. The infiltration rate was also measured in the field using a double ring infiltrometer [24]. Upon bringing the soil samples to the laboratory, they were air-dried, gently ground to pass through a 2-mm sieve, and kept in plastic containers until use. The hydrology tool inside the Spatial Analysis Tools of ArcGIS, version 10.7, is used to delineate the basin boundaries, map the drainage networks, and extract topographic data [25].

## 2.3 Soil Erodibility Indices

Apart from soil erodibility modelling, several indices were also used to explore the proneness of soil to erosion.

### 2.3.1 Dispersion Ratio (DR)

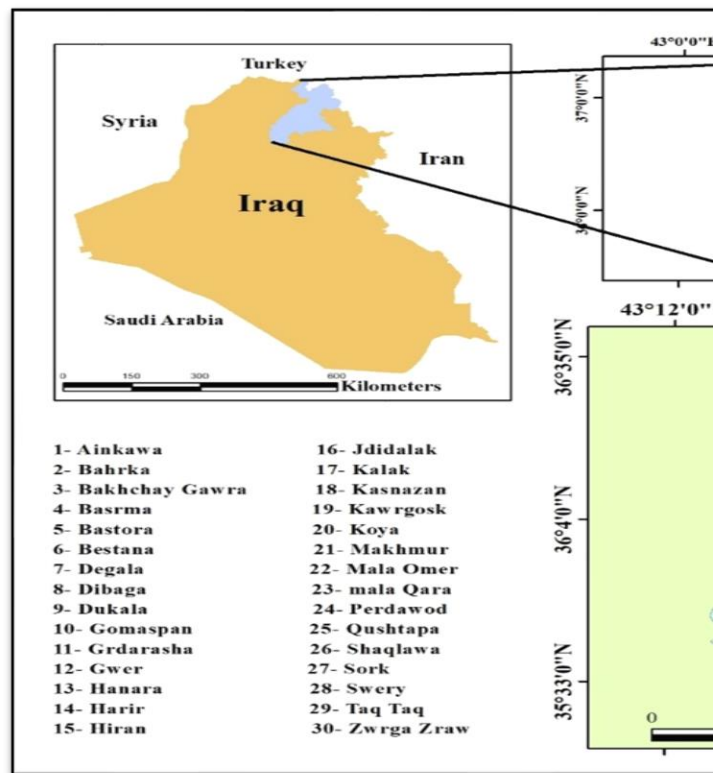
It was determined by the procedure outlined by Akhtaruzzaman et al. [20] and calculated according to the following model:

$$DR = \frac{A}{B} \quad (1)$$

where A = % water-dispersible silt-plus-clay; B = % actual silt-plus-clay determined during particle size analyses with Calgon.

### 2.3.2 Clay Ratio (CR)

The calculation of this index was based on the following equation [7]:



**Figure 2:** Location map showing the sampling sites.

$$CR = \frac{\% \text{ silt} + \% \text{ sand}}{\% \text{ clay}} \quad (2)$$

### 2.3.3 Modified Clay Ratio (MCR)

Clay ratio was modified according to the following equation to better explain the variability of soil erodibility <sup>[26]</sup>.

$$MCR = \frac{\% \text{ silt} + \% \text{ sand}}{\% \text{ clay} + \% \text{ organic matter}} \quad (3)$$

### 2.3.4 Structural Stability Index (SSI)

It was developed by Pieri <sup>[27]</sup> as an index of structural stability according to the following expression:

$$SSI = \frac{\% \text{ Soil organic matter}}{\% \text{ silt} + \% \text{ clay}} \times 100 \quad (4)$$

The above equation was also used for the critical level of soil organic matter (CLOM).

**Table 1:** Sampling locations and types of land uses, along with their geographic coordinates.

| No. | Sites          | Latitude | Longitude | Types of land use |
|-----|----------------|----------|-----------|-------------------|
| 1   | Ainkawa        | 36.2488° | 43.9949°  | Crop land         |
| 2   | Bahrka         | 36.3663° | 44.0175°  | Crop land         |
| 3   | Bakhchay Gawra | 36.2201° | 44.2306°  | Grazing land      |
| 4   | Basrma         | 36.5405° | 44.3233°  | Crop land         |
| 5   | Bastora        | 36.3266° | 44.2055°  | Forest land       |
| 6   | Bestana        | 36.0324° | 44.1913°  | Crop land         |
| 7   | Degala         | 36.1742° | 44.3911°  | Grazing land      |
| 8   | Dibaga         | 35.8375° | 43.8272°  | Crop land         |
| 9   | Dukala         | 35.9363° | 43.9516°  | Crop land         |

|    |            |          |          |              |
|----|------------|----------|----------|--------------|
| 10 | Gomaspan   | 36.2731° | 44.2974° | Crop land    |
| 11 | Grdarasha  | 36.1088° | 44.0122° | Crop land    |
| 12 | Gwer       | 36.0988° | 43.5442° | Crop land    |
| 13 | Hanara     | 36.3005° | 44.2376° | Forest land  |
| 14 | Harir      | 36.5339° | 44.3568° | Crop land    |
| 15 | Hiran      | 36.2818° | 44.5151° | Forest land  |
| 16 | Jdidalak   | 35.9652° | 43.8792° | Crop land    |
| 17 | Kalak      | 36.2822° | 43.6523° | Grazing land |
| 18 | Kasnazan   | 36.2174° | 44.1786° | Grazing land |
| 19 | Kawrgosk   | 36.3521° | 43.7871° | Crop land    |
| 20 | Koya       | 36.0756° | 44.6443° | Crop land    |
| 21 | Makhmur    | 35.7838° | 43.5547° | Crop land    |
| 22 | Mala Omer  | 36.2866° | 44.1241° | Crop land    |
| 23 | Mala Qara  | 36.0081° | 43.5398° | Crop land    |
| 24 | Perdawod   | 36.0119° | 43.9372° | Crop land    |
| 25 | Qushtapa   | 35.9881° | 44.0475° | Crop land    |
| 26 | Shaqlawaw  | 36.4255° | 44.3616° | Crop land    |
| 27 | Sork       | 36.4151° | 44.3197° | Forest land  |
| 28 | Swery      | 36.1604° | 43.9028° | Crop land    |
| 29 | Taq Taq    | 35.8797° | 44.5834° | Crop land    |
| 30 | Zwrga Zraw | 35.9122° | 43.8481° | Grazing land |

## 2.4 Comparison of Previously Published Models for Assessing Soil Erodibility

The soil erodibility at each sampling point was assessed using the following formula by Wischmeier and Smith <sup>[5]</sup> as a reference model to check the power of predictability of previously published and proposed models.

### 2.4.1 Wischmeier and Smith, 1978 Model (Reference Model)

$$K_1 = 2.77 \times 10^{-6} M^{1.14} (12 - OM) + 0.043 (SC - 2) + 0.033 (PC - 3) \quad (5)$$

$K_1$  = Soil erodibility (metric unit) from reference model

$M$  = (% silt + % very fine sand) (100 - % clay)

$OM$  = Soil organic matter content (%)

$SC$  = Structure class code (-)

$PC$  = Permeability class code (-)

### 2.4.2 Wischmeier and Smith, 1978, after Truncating the Permeability Term

$$K_2 = 2.77 \times 10^{-6} M^{1.14} (12 - OM) + 0.043 (SC - 2) \quad (6)$$

### 2.4.3 EPIC Model Developed by Sharpley and Williams <sup>[11]</sup>

$$K_3 = 0.1317 A_x B_x C_x D \quad (7)$$

$$A = 0.2 + 0.3 \exp \left( -0.0256 SAN \left( 1 - \frac{SIL}{100} \right) \right)$$

$$B = \left( \frac{SIL}{CLA + SIL} \right)^{0.3}$$

$$C = \left( 1 - \frac{0.25 C}{C + \exp(3.72 - 2.95C)} \right)$$

$$D = \left( 1 - \frac{0.70 SN1}{SN1 + \exp(-5.41 + 22.9SN1)} \right)$$

where:  $SAN$  = %Sand,  $SIL$  = % silt,  $CLA$  = % clay,  $C$  = % soil organic carbon and  $SN1$  = (1- $SAN/100$ ).

### 2.4.4 Torri (Torri et al., 1997) <sup>[28]</sup>

$$K_4 = 0.0293 (0.65 - D_g + 0.24 D_g^2) * \exp(-0.0021 \left(\frac{SOM}{C}\right) - 0.00037 \left(\frac{SOM}{C}\right)^2 - 4.02C + 1.72C^2) \quad (8)$$

Where:

$$D_g = \sum f_i \log(\sqrt{d_i d_{i-1}})$$

$D_g$  = The geometric mean diameter (mm)

$d_i$  = The maximum diameter of the  $i$ th class (mm). The maximum diameters for sand, silt, and clay are 2, 0.05, and 0.002 mm, respectively

$d_{i-1}$  = The minimum diameter of the  $i$ th class in mm. The minimum diameters for sand, silt, and clay are 0.05, 0.002, and 0.00005 mm, respectively

$f_i$  = The mass fraction of the  $i$ th class (-)

SOM = % Soil organic matter

C = The mass fraction of clay (-)

$K_4$  = The soil erodibility in SI unit

#### 2.4.5 Shirazi et al. (1988) [29]

$$K_5 = 7.594 \left\{ 0.0034 + 0.0405 \exp \left[ -\frac{1}{2} \left[ \frac{\log(D_g) + 1.659}{1.7101} \right]^2 \right] \right\} \quad (9)$$

$$D_g(\text{mm}) = \exp(0.01 \sum f_i \ln m_i)$$

where  $f_i$  = percent of soil separates,  $m_i$  = the arithmetic diameter of the particle size limit

$D_g$  = Geometric mean diameter of the soil particles (mm)

#### 2.4.6 The Proposed Pedotransfer Function during the Current Study

$$K_6 = 1.5173 - 0.0079SI - 0.0327CLOM - 0.0357FC \quad (10)$$

$$FC = 13.29 + 0.379 C \quad \text{by Karim}^{[30]}$$

where:

$K_6$  = Soil erodibility in metric units

SI = Silt content (%)

CLOM = critical level of soil organic matter (-)

FC = Water retention at -33kPa

C = % percent clay

### 2.5 Evaluation of Models Performance

The following metrics have been used to test the performance of the commonly used and proposed models to predict the soil erodibility [31,32]:

$$MBE = \frac{1}{N} \sum_{i=1}^N (O_i - P_i) \quad (11)$$

$$MAE = \frac{1}{N} \sum_{i=1}^N |O_i - P_i| \quad (12)$$

$$PE = \frac{1}{N} \sum_{i=1}^N \left| \frac{O_i - P_i}{O_i} \right| \times 100 \quad (13)$$

$$MRSE = \sqrt{\frac{\sum (O_i - P_i)^2}{N}} \quad (14)$$

$$R = \frac{\sum (x_i - \bar{x})(y_i - \bar{y})}{\sqrt{\left( \sum x_i^2 - \frac{(\sum x_i)^2}{N} \right) \left( \sum y_i^2 - \frac{(\sum y_i)^2}{N} \right)}} \quad (15)$$

$$D = \sqrt{\frac{\sum (x_i - \bar{x})^2}{N}} \quad (16)$$

$$NSE = 1 - \frac{\sum_{i=1}^n (O_i - P_i)^2}{\sum_{i=1}^n (O_i - \bar{O}_i)^2} \quad (17)$$

$$MSEc = \left[ \frac{\sum [(P_i - \bar{P}) - (O_i - \bar{O})]^2}{N - 1} \right]^{-0.5} \quad (18)$$

$$d = 1 - \frac{\sum_{i=1}^N (P_i - O_i)^2}{\sum_{i=1}^N (|O_i - \bar{O}| + |P_i - \bar{P}|)^2} \quad (19)$$

$$CRM = \frac{\sum O_i - \sum P_i}{\sum O_i} \quad (20)$$

where: N = number of data points;  $O_i$  = observed values;  $P_i$  = predicted values;  $\bar{O}$  = mean of observed values;  $\bar{P}$  = mean predicted value; MBE = mean biased error; MAE = mean absolute error; MAPE = mean absolute percentage error; RMSE

= root mean square error;  $r$  = Pearson correlation coefficient; SD = standard deviation; NSE= Nash-Sutcliffe efficiency; RMSEc = Centered root mean square error;  $d$  = coefficient of agreement and CRM= coefficient of residual mass.

The degree of correspondence between the modeled and reference behavior was also quantified in terms of standard deviation. Root mean square error and the Pearson correlation coefficient are collectively considered as the main parameters of the Taylor diagram <sup>[33]</sup>.

## 2.6 Generation of Continuous Surfaces for Soil Erodibility

To generate soil erodibility at unsampled locations, the values of soil erodibility of the geo-coded sampling points estimated by 6 soil erodibility models were interpolated by the IDW interpolation method in GIS Environment using ArcGIS Ver. 10.7. The outputs were used to generate maps for soil erodibility and presented in figures.

## 3 Results and Discussion

### 3.1 Basic Soil Characteristics

Table 2 presents the input variables required for estimating soil erodibility and other influencing properties for soil samples obtained at different locations and under different land uses over the study area. It is evident from the displayed results that the area under investigation is characterized by having a wide range of soil textures, varying from sandy loam to clay soils. The dominant soil textures are silt, clay loam and clay loam and silt loam. Table 2 also displays the descriptive statistics for these

variables. As can be seen in Table 2 that the sand content varied from a minimum of 5.64% to a maximum of 57.21% with a mean of 22.16%; the silt varied between 30.66% and 64.72%, while the clay ranged between 9.90% to 45.41%, and it differed from 9.90% to 45.41% for clay content. It was also observed that the soil organic matter content ranged from as low as 0.48% to as high as 2.98% and for VFS from 0.68% to 8.04%, while the infiltration rate ranged between 1.1 and 8.76 cm hr<sup>-1</sup>, water retention at – 33 kPa between 17.04% and 30.50% and lime equivalent varied from 26.5% to 47.5%. Regarding soil bulk density ranged between 1.16 and 1.42 Mg m<sup>-3</sup> and the mean weight diameter from 0.33 to 4.93 mm. Furthermore, the results showed that the sand content exhibited the highest coefficient of variation, CV (62.42%), followed by infiltration rate (61.14%) and Mean weight diameter, MWD (50.37%). Contrarily, the bulk density offered the least value for CV (4.67%), and lime equivalent offered the second lowest value (14.39%). Based on the classification scheme proposed by Wilding <sup>[34]</sup>, each of sand, VFS, organic matter, infiltration rate, MWD, and dispersion ratio was put under a high class of variability (CV > 35%) (Table 3). In contrast, each of bulk density and equivalent lime was put under the low class of variability (CV < 15), while the rest of the study variables fell within the moderate class (15% < CV < 35%).

The skewness results revealed that with 2 exceptions, the skewness of the study variables is between -1 and 1, indicating that the data sets are normally distributed. Further, the negative and positive skewness indicate that the datasets tail to the left and to the right, respectively, on the horizontal axis. Additionally, it can be noticed that based on the obtained values of the kurtosis that there are some deviations from the normal distribution of the data sets.

**Table 2:** Some selected physical and chemical properties of the soils at different sites over the study area.

| Site           | Particle size distribution (%) |       |       | VFS (%) | Texture class | Bulk density (Mg m <sup>-3</sup> ) | Organic matter (%) | Infiltration rate (cm hr <sup>-1</sup> ) | Water retention at - 33 kpa | MWD (mm) | Dispersion ratio | E-CaCO <sub>3</sub> Equivalent (%) | K (metric unit) |
|----------------|--------------------------------|-------|-------|---------|---------------|------------------------------------|--------------------|------------------------------------------|-----------------------------|----------|------------------|------------------------------------|-----------------|
|                | Sand                           | Silt  | Clay  |         |               |                                    |                    |                                          |                             |          |                  |                                    |                 |
| Ainkawa        | 12.35                          | 45.95 | 41.70 | 4.53    | SiL           | 1.31                               | 1.53               | 2.72                                     | 29.09                       | 1.38     | 16.55            | 39.10                              | 0.26            |
| Bahrka         | 8.19                           | 53.67 | 38.15 | 1.53    | SiCL          | 1.24                               | 1.31               | 2.35                                     | 27.75                       | 3.27     | 10.16            | 37.00                              | 0.32            |
| Bakhchay Gawra | 20.66                          | 44.21 | 35.14 | 2.47    | CL            | 1.26                               | 1.25               | 3.26                                     | 26.61                       | 1.41     | 19.59            | 47.50                              | 0.32            |
| Basrma         | 23.49                          | 38.35 | 38.16 | 1.69    | CL            | 1.28                               | 2.40               | 2.87                                     | 27.75                       | 3.41     | 24.38            | 38.26                              | 0.20            |
| Bastora        | 26.23                          | 36.77 | 37.01 | 2.99    | CL            | 1.33                               | 2.98               | 1.10                                     | 27.32                       | 1.39     | 14.05            | 41.20                              | 0.22            |
| Bestana        | 13.94                          | 48.75 | 37.31 | 4.06    | SiCL          | 1.20                               | 0.73               | 2.67                                     | 27.43                       | 1.12     | 16.86            | 34.90                              | 0.36            |
| Degala         | 26.20                          | 44.70 | 29.11 | 8.04    | CL            | 1.24                               | 1.09               | 2.15                                     | 24.32                       | 2.40     | 32.29            | 43.30                              | 0.44            |
| Dibaga         | 48.50                          | 35.08 | 16.43 | 5.55    | L             | 1.42                               | 0.63               | 4.99                                     | 19.52                       | 3.66     | 40.24            | 37.00                              | 0.33            |

|               |           |           |           |          |      |      |      |      |       |      |       |       |      |
|---------------|-----------|-----------|-----------|----------|------|------|------|------|-------|------|-------|-------|------|
| Dukala        | 13.9<br>4 | 56.3<br>3 | 29.7<br>3 | 0.6<br>8 | SiCL | 1.36 | 1.06 | 1.92 | 24.56 | 3.67 | 16.86 | 32.80 | 0.42 |
| Gomaspa<br>n  | 9.06      | 49.7<br>5 | 41.1<br>9 | 1.5<br>4 | SiC  | 1.30 | 1.23 | 1.88 | 28.90 | 0.71 | 14.81 | 34.90 | 0.31 |
| Grdarash<br>a | 12.9<br>3 | 52.2<br>5 | 34.8<br>2 | 3.5<br>1 | SiCL | 1.27 | 1.14 | 2.42 | 26.49 | 0.33 | 34.51 | 37.00 | 0.39 |
| Gwer          | 18.9<br>5 | 53.0<br>8 | 27.9<br>7 | 2.7<br>2 | SiCL | 1.21 | 1.33 | 3.70 | 23.89 | 2.44 | 24.29 | 37.00 | 0.42 |
| Hanara        | 5.64      | 57.0<br>2 | 37.3<br>4 | 0.9<br>5 | SiCL | 1.36 | 0.86 | 1.82 | 27.44 | 0.77 | 14.28 | 30.70 | 0.47 |
| Harir         | 8.12      | 51.8<br>9 | 39.9<br>9 | 3.1<br>2 | SiCL | 1.26 | 1.12 | 3.05 | 28.45 | 1.02 | 22.56 | 37.00 | 0.35 |
| Hiran         | 49.8<br>5 | 40.2<br>5 | 9.90      | 1.6<br>2 | L    | 1.39 | 2.65 | 2.61 | 17.04 | 4.93 | 28.93 | 35.74 | 0.31 |
| Jdidalak      | 11.9<br>6 | 64.4<br>6 | 23.5<br>7 | 5.8<br>7 | SiL  | 1.28 | 0.89 | 3.16 | 22.22 | 2.74 | 22.36 | 32.80 | 0.55 |
| Kalak         | 57.2<br>1 | 32.4<br>2 | 10.3<br>6 | 4.5<br>9 | SL   | 1.32 | 1.64 | 8.76 | 17.22 | -    | 48.44 | 30.70 | 0.35 |
| Kasnazan      | 34.2<br>6 | 30.6<br>6 | 35.0<br>8 | 3.3<br>7 | CL   | 1.33 | 1.47 | 1.16 | 26.59 | 4.06 | 28.37 | 43.30 | 0.22 |
| Kawrgos<br>k  | 20.6<br>9 | 50.2<br>1 | 29.1<br>1 | 5.1<br>1 | CL   | 1.33 | 0.99 | 1.32 | 24.32 | 2.98 | 11.76 | 37.00 | 0.46 |
| Koya          | 17.7<br>3 | 48.1<br>4 | 34.1<br>2 | 4.0<br>5 | SiCL | 1.34 | 1.41 | 1.47 | 26.22 | 4.57 | 30.23 | 43.30 | 0.39 |
| Makhmur       | 11.8<br>5 | 57.1<br>8 | 30.9<br>7 | 5.6<br>7 | SiCL | 1.28 | 0.87 | 1.17 | 25.03 | 2.67 | 9.40  | 26.50 | 0.51 |
| Mala<br>Omer  | 19.7<br>1 | 35.1<br>5 | 45.1<br>4 | 4.1<br>2 | C    | 1.32 | 0.65 | 1.95 | 30.40 | 1.04 | 24.52 | 32.80 | 0.23 |
| Mala<br>Qara  | 33.7<br>2 | 44.0<br>8 | 22.2<br>0 | 4.0<br>4 | L    | 1.31 | 1.01 | 2.01 | 21.70 | 1.78 | 35.96 | 28.60 | 0.36 |
| Perdawod      | 11.9<br>7 | 64.7<br>2 | 23.3<br>1 | 5.0<br>2 | SiL  | 1.28 | 0.61 | 1.99 | 22.13 | 3.54 | 21.19 | 34.90 | 0.64 |
| Qushtapa      | 13.9<br>2 | 49.1<br>9 | 36.8<br>9 | 5.3<br>5 | SiCL | 1.24 | 1.22 | 1.35 | 27.27 | 3.30 | 28.89 | 43.30 | 0.40 |
| Shaqlawaa     | 12.7<br>6 | 41.8<br>3 | 45.4<br>1 | 2.2<br>1 | SiC  | 1.33 | 2.21 | 2.35 | 30.50 | 3.06 | 34.45 | 26.50 | 0.24 |
| Sork          | 23.1<br>6 | 51.2<br>5 | 25.5<br>8 | 4.3<br>9 | SiL  | 1.16 | 0.48 | 3.26 | 22.99 | 2.20 | 12.14 | 32.80 | 0.51 |
| Swery         | 17.2<br>2 | 53.7<br>6 | 29.0<br>2 | 3.7<br>2 | SiCL | 1.23 | 1.18 | 1.98 | 24.29 | 4.75 | 18.78 | 37.00 | 0.47 |
| Taq Taq       | 50.2<br>4 | 36.2<br>3 | 13.5<br>3 | 2.3<br>6 | L    | 1.39 | 0.73 | 6.47 | 18.42 | 2.02 | 70.81 | 32.80 | 0.38 |
| Zwrga<br>Zraw | 30.2<br>3 | 50.2<br>7 | 19.5<br>0 | 3.9<br>6 | SiL  | 1.35 | 0.76 | 1.73 | 20.68 | 4.00 | 7.43  | 43.30 | 0.56 |

SiL = Silty Loam, SiCL = Silty Clay Loam, CL = Clay Loam,

L = Loam, SiC = Silty Clay, SL = Sandy Loam, C=Clay

**Table 3:** Descriptive Statistics for the study input variables used for estimating soil erodibility.

| Variable | Unit | Sample size (N) | Range | Min | Max | Mean | SD | Variance | CV (%) | Skewness | Kurtosis |
|----------|------|-----------------|-------|-----|-----|------|----|----------|--------|----------|----------|
|----------|------|-----------------|-------|-----|-----|------|----|----------|--------|----------|----------|

|                   |                     |    |       |       |       |       |       |        |       |       |        |
|-------------------|---------------------|----|-------|-------|-------|-------|-------|--------|-------|-------|--------|
| MWD               | Mm                  | 30 | 4.6   | 0.33  | 4.93  | 2.56  | 1.29  | 1.66   | 50.37 | 0.09  | - 0.98 |
| Sand              | %                   | 30 | 51.57 | 5.64  | 57.21 | 22.16 | 13.83 | 191.28 | 62.42 | 1.24  | 0.72   |
| Silt              | %                   | 30 | 34.06 | 30.66 | 64.72 | 47.25 | 8.90  | 79.15  | 18.83 | -0.05 | - 0.51 |
| Clay              | %                   | 30 | 35.51 | 9.90  | 45.41 | 30.59 | 9.78  | 95.74  | 31.99 | -0.62 | - 0.35 |
| VFS               | %                   | 30 | 7.36  | 0.68  | 8.04  | 3.63  | 1.68  | 2.81   | 46.25 | 0.32  | 0.20   |
| Bulk density      | Mg m <sup>-3</sup>  | 30 | 0.26  | 1.16  | 1.42  | 1.30  | 0.06  | 0.00   | 4.67  | -0.19 | - 0.20 |
| Organic matter    | %                   | 30 | 2.50  | 0.48  | 2.98  | 1.25  | 0.61  | 0.37   | 48.70 | 1.44  | 1.85   |
| Infiltration rate | mm hr <sup>-1</sup> | 30 | 7.66  | 1.10  | 8.76  | 2.65  | 1.62  | 2.63   | 61.14 | 2.40  | 6.83   |
| Dispersion ratio  | %                   | 30 | 63.38 | 7.43  | 70.81 | 24.50 | 13.19 | 174.04 | 53.84 | 1.63  | 4.09   |
| Lime Equivalent   | %                   | 30 | 21.00 | 26.50 | 47.50 | 36.30 | 5.22  | 27.28  | 14.39 | 0.09  | - 0.31 |
| Soil erodibility  | Metric unit         | 30 | 0.44  | 0.20  | 0.64  | 0.38  | 0.11  | 0.01   | 29.08 | 0.31  | - 0.31 |

### 3.2 Descriptive Statistics of Soil Erodibility Estimated by Different Models

Table 4 exhibits the summary of statistics for the estimated values of soil erodibility by different formulas, namely Wischmeier and Smith, 1978 (K1), truncated Wischmeier and Smith (K2); EPIC (K3), Torri et al., 1997 (K4), Shirazi et al., 1988 (K5) and the proposed model (K6) during the current study. The soil erodibility dataset estimated by the Wischmeier and Smith (1978) model, which hereafter is referred to as the reference method, varied from a minimum of 0.197 to a maximum of 0.637 with a mean of 0.38 metric unit  $[(t/ha) \cdot \frac{ha \cdot hr}{metric \ ton \cdot m \cdot cm}]$ . It can also be noticed that it ranges from 0.187 to 0.604 for the Truncated Wischmeier and Smith, from 0.231 to 0.431 for Shirazi et al., 1988, from 0.291 to 0.485 for Torri et al., 1987, from 0.300 to 0.559 for the EPIC, and from 0.179 to 0.596 metric unit for the

proposed model. The results also disclosed that the reference method offered the highest range, followed by the Truncated Wischmeier and Smith (1978) model and the proposed model. In contrast, the Torri et al. <sup>[35]</sup> model offered the lowest range, followed by Shirazi et al. (1988) and EPIC models. Additionally, It can be observed from the results of Table 4 that the Truncated Wischmeier and Smith offered the highest coefficient of variation, CV (29.450%), followed by the reference method (29.083%) and the proposed model (27.406%). Contrarily, the Shirazi et al. <sup>[29]</sup> model gave the lowest value for CV (13.327%), followed by the Torri et al. <sup>[28]</sup> (13.625%) and the EPIC model (15.510%). The skewness results also revealed that, with one exception, the data generated by different models are sandwiched between -1 and 1, indicating that the generated data by most of the models follow a normal distribution. A dataset may be considered as normally distributed if the skewness value ranges from -1 to 1 <sup>[36]</sup>.

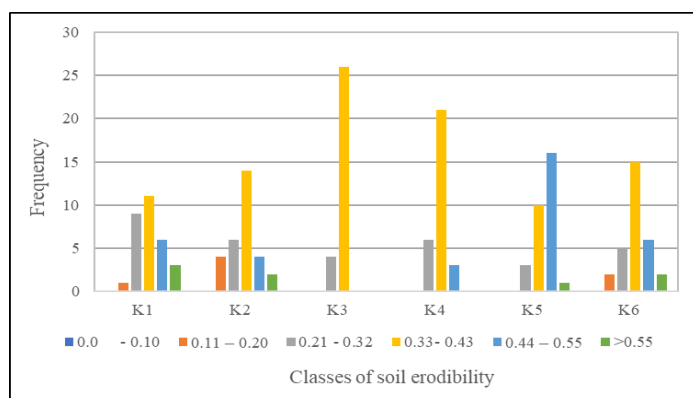
**Table 4:** Descriptive Statistics for soil erodibility estimated by different models.

| Model                             | N  | Range | Min   | Max   | Mean  | Standard Deviation | Variance | CV (%) | Skewness | Kurtosis |
|-----------------------------------|----|-------|-------|-------|-------|--------------------|----------|--------|----------|----------|
| 1. Wischmeier and Smith           | 30 | 0.440 | 0.197 | 0.637 | 0.380 | 0.110              | 0.012    | 29.083 | 0.311    | -0.312   |
| 2. Truncated Wischmeier and Smith | 30 | 0.417 | 0.187 | 0.604 | 0.367 | 0.108              | 0.012    | 29.450 | 0.089    | -0.308   |
| 3.(Shirazi et al., 1988           | 30 | 0.200 | 0.231 | 0.431 | 0.394 | 0.053              | 0.003    | 13.327 | -2.000   | 3.294    |

|                      |    |       |       |       |       |       |       |        |        |        |
|----------------------|----|-------|-------|-------|-------|-------|-------|--------|--------|--------|
| 4.Torri et al., 1997 | 30 | 0.194 | 0.291 | 0.485 | 0.377 | 0.051 | 0.003 | 13.625 | 0.311  | -0.468 |
| 5. EPIC model        | 30 | 0.259 | 0.300 | 0.559 | 0.439 | 0.068 | 0.005 | 15.510 | -0.388 | -0.484 |
| 6. Proposed model    | 30 | 0.417 | 0.179 | 0.596 | 0.379 | 0.104 | 0.011 | 27.406 | -0.119 | -0.015 |

### 3.3 Soil Classification Based on Estimated Soil Erodibility Index

Based on the estimated values of erodibility index, the soils of the investigated sites were categorized into different groups according to the scheme shown by Castro et al. [37] and the results are presented in Figure 3. It is apparent from the displayed results that the fairly high class (0.33- 0.43) offered the highest frequency for the generated data of 5 out of 6 models. It can also be observed that the proposed model (K6) offered a distribution very close to a normal distribution, followed by the Wiscmeier and Smith [5] model (K1) and the truncated Wiscmeier and Smith (K<sub>2</sub>).

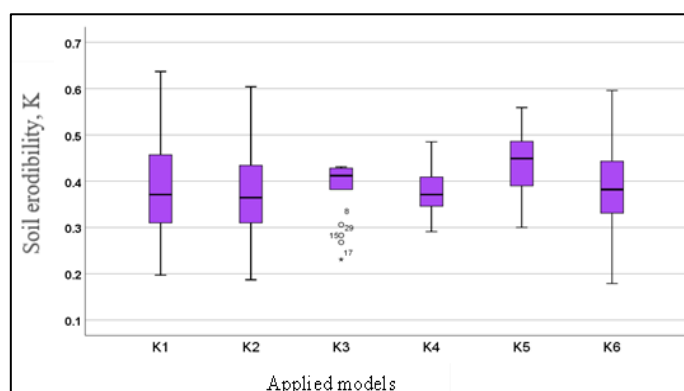


**Figure 3:** Frequency distribution of soil erodibility estimated by the K1 model.

Unlike these models, the estimated soil erodibility values estimated by some models, such as Sherazi et al. [29] (K3) and Torri et al. [35] (K4), were highly deviated from a normal distribution. It is also interesting to note that none of the studied soils fell in the very low class (0.0 - 0.10).

When the soils of the investigated area were classified into groups based on the estimated soil erodibility by the reference method, 67% of soils fell in the moderate (0.21- 0.32) and fairly high (0.33 - 0.43) classes. The results also indicated that 10% and 20% of the soils were in the high (0.44 -0.55) and very high ( > 0.55) classes, respectively. On the other hand, it was noticed that about 3% and 0% of the study soils fell in low (0.10 - 0.20) and very low (0.00 - 0.10 m) classes, respectively.

To further confirm the authenticity of the distribution of the generated data by the applied models, a Box-Whisker plot was shown in Figure 4. As the median line of K6 and K2 is located at the center of the box, it indicates that these models produced more symmetrical data compared to the remaining models. The existence of some points outside the inner and outer fences of the K3 model is indicative of the presence of extreme points in the data sets of Shirazi et al. [29] model. Furthermore, it can be seen that the K1 model has the longest length, followed by K2 and K6. The length of the box is an indicator of data range; the longer the box, the wider the data range or variability.



**Figure 4:** Representation of estimated soil erodibility by Box-Whisker plot.

### 3.4 Soil Erodibility Indices

In the current study, an additional attempt was made to determine 4 commonly used erodibility indices for identifying the proneness of the investigated soils to erosion (Table 5). These indices encompassed clay ratio (CR), Truncated clay ratio (MCR), dispersion ratio (DR), and critical level of soil organic matter content (CLOM). As can be noticed in Table 5, the estimated values fall in the following ranges: CR, 1.202 – 9.099; MCR, 1.146- 7.47; DR, 7.426 – 70.807; and CROM, 0.625 – 5.278. The lowest values for CR, MCR, DR, and CLOM were observed in Shaqlawa, Shaqlawa, Zwrga Zraw, and Sork, respectively. On the other hand, the highest values were observed in Hiran, Kalak, Taq Taq, and Hiran, respectively. The results also revealed that more than 96% of the investigated soils had CROM of less than 5, indicating that the majority of the soils have no stable structure

and do not offer resistance to erosion <sup>[38]</sup>. It is also apparent from the displayed results that more than 73% of sampling sites have a dispersion ratio of more than 15% thereby indicating that the majority of the soils are highly vulnerable to erosion <sup>[26]</sup>. It is

commendable to mention that the above study indices are appropriate to estimate the soil vulnerability to erosion, where physical measurement is very difficult.

**Table 5:** Some selected erodibility indices for different sites over the study area.

| Site           | Dispersion ratio | Clay ratio | Modified clay ratio | Critical level of organic matter |
|----------------|------------------|------------|---------------------|----------------------------------|
| Ainkawa        | 16.552           | 1.398      | 1.349               | 1.742                            |
| Bahrka         | 10.158           | 1.622      | 1.568               | 1.431                            |
| Bakhchay Gawra | 19.591           | 1.846      | 1.783               | 1.572                            |
| Basrma         | 24.379           | 1.620      | 1.524               | 3.136                            |
| Bastora        | 14.047           | 1.702      | 1.575               | 4.041                            |
| Bestana        | 16.857           | 1.680      | 1.648               | 0.846                            |
| Degala         | 32.293           | 2.436      | 2.348               | 1.471                            |
| Dibaga         | 40.241           | 5.087      | 4.899               | 1.223                            |
| Dukala         | 16.858           | 2.363      | 2.282               | 1.228                            |
| Gomaspan       | 14.813           | 1.428      | 1.386               | 1.348                            |
| Grdarasha      | 34.513           | 1.872      | 1.813               | 1.303                            |
| Gwer           | 24.292           | 2.575      | 2.458               | 1.641                            |
| Hanara         | 14.277           | 1.678      | 1.641               | 0.911                            |
| Harir          | 22.557           | 1.501      | 1.460               | 1.217                            |
| Hiran          | 28.928           | 9.099      | 7.180               | 5.278                            |
| Jdidalak       | 22.364           | 3.242      | 3.124               | 1.013                            |
| Kalak          | 48.440           | 8.650      | 7.470               | 3.826                            |
| Kasnazan       | 28.372           | 1.851      | 1.776               | 2.234                            |
| Kawrgosk       | 11.759           | 2.436      | 2.356               | 1.249                            |
| Koya           | 30.231           | 1.931      | 1.854               | 1.710                            |
| Makhmur        | 9.405            | 2.229      | 2.169               | 0.984                            |
| Mala Omer      | 24.524           | 1.215      | 1.198               | 0.806                            |
| Mala Qara      | 35.961           | 3.505      | 3.352               | 1.527                            |
| Perdawod       | 21.189           | 3.289      | 3.206               | 0.688                            |
| Qushtapa       | 28.892           | 1.711      | 1.656               | 1.418                            |
| Shaqlawla      | 34.446           | 1.202      | 1.146               | 2.533                            |
| Sork           | 12.138           | 2.909      | 2.855               | 0.625                            |
| Swery          | 18.777           | 2.445      | 2.349               | 1.430                            |
| Taq Taq        | 70.807           | 6.389      | 6.064               | 1.461                            |
| Zwrga Zraw     | 7.426            | 4.128      | 3.973               | 1.094                            |

### 3.5 Pearson's Correlation Coefficient for the Relationship between Soil Erodibility and each of the Input Variables and Erodibility Indices

Table 6 presents the correlation coefficient between soil erodibility (K) estimated by the reference method (K1) and the input variables and some selected erodibility indices. As can be noticed in Table 6, each of silt, VFS, and MWD was positively

correlated with soil erodibility. In contrast, the remaining variables were negatively correlated with K. It can also be observed that the correlation between K and clay content was negative and highly significant ( $r = -0.415^*$ ). Similarly, its correlation with organic matter was negative and very highly significant ( $r = -0.621^{**}$ ). Contrarily, the soil erodibility was positively and highly significantly correlated with each of silt and VFS.

**Table 6:** Pearson's correlation coefficient for the relationship between soil erodibility and each of the input variables and some selected erodibility indices.

| Input variable                  | Sand             | Silt    | Clay       | VFS   | Bulk density        | Organic matter | Infiltration rate                | Lime equivalent | MWD   |
|---------------------------------|------------------|---------|------------|-------|---------------------|----------------|----------------------------------|-----------------|-------|
| Pearson Correlation Coefficient | - 0.197          | 0.762** | - 0.415    | 0.389 | - 0.247             | - 0.621        | - 0.064                          | - 0.132         | 0.176 |
| Erodibility indices             | Dispersion ratio |         | Clay ratio |       | Modified clay ratio |                | Critical level of organic matter |                 |       |
| Pearson Correlation Coefficient | - 0.220          |         | 0.129      |       | 0.181               |                | - 0.532                          |                 |       |

It is also obvious from Table 6 that each clay ratio and truncated clay ratio were found to be positively correlated with K, while it was negatively correlated with each of the dispersion ratio and critical level of organic matter (CLOM). Among these indices, only CLOM was high significantly correlated with K ( $r = -0.532^*$ ) at  $N = 30$  and  $P = 0.05$ . It is commendable to mention that the last index was considered as one of the input variables of the proposed model during the current study because of its strong correlation with K.

Table 7 displays the mean soil erodibility estimated by different models under different land uses. As can be seen in Table 7, irrespective of the type of model for K estimation and with one exception, the forest land offered the lowest value for K, while the cropland offered the highest value for K. It is noteworthy to indicate that land use type did not yield a significant difference in K. The estimated K values by some models, such as EPIC and the proposed one, exhibited better harmony with land use change compared to the estimated K value by the remaining model, indicating the appropriateness of the last two models (K5 and K6) for K estimation.

### 3.6 Soil Erodibility as Affected by Land Use

**Table 7:** Soil erodibility as affected by different land uses over the study area.

| Land Use     | Wischmeier and Smith | Truncated Wischmeier and Smith | Shirazi et al. (1988) | Torri et al. (1997) | EPIC model | Proposed model |
|--------------|----------------------|--------------------------------|-----------------------|---------------------|------------|----------------|
| Cropland     | 0.380                | 0.367                          | 0.400                 | 0.379               | 0.454      | 0.391          |
| Forestland   | 0.378                | 0.361                          | 0.377                 | 0.366               | 0.421      | 0.358          |
| Grazing land | 0.379                | 0.372                          | 0.382                 | 0.378               | 0.390      | 0.344          |

### 3.7 Description of the Proposed Model during the Current Study

As mentioned earlier, one objective of the current study was to develop a model for estimating soil erodibility based on linear

regression analysis. The result of this analysis indicated that the following model was the best model for predicting soil erodibility over the study area:

$$K6 = 1.517 - 0.0079 \% \text{ Silt} - 0.0327 \text{ CLOM} - 0.0357 \text{ FC} \quad N = 30 \quad R^2 = 0.884 \quad (21)$$

where: K6 = soil erodibility estimated by the proposed model

FC = Soil water retention at – 33 kPa.

It is evident from the above analysis that the variation in silt, CLOM, and FC accounted for more than 88% of the variation in soil erodibility. This is an indication of a good match between the estimated K by the proposed and the reference model. The maximum correlation between each pair of the input variables in this model was - 0.768. Multicollinearity analysis revealed that the condition number (CN) was 3.495, indicating that a low linear multicollinearity exists (CN < 20).

### 3.8 Evaluation of the Study Models for Estimating Soil Erodibility

Model evaluation was accomplished by comparing the estimated values by the reference method (K1) with the predicted values by K2, K3, K4, K5, and K6 models. To achieve this objective, the estimated values by the reference method were plotted versus the predicted values by each of these models in relation to line 1:1, and the results are portrayed in Figure 5. It can be discerned from the plotted figure that the K2 model offered the best performance, followed by the K6 model. The plotted points belonging to these 2 models fall on or close to the line 1:1 over the entire range of the estimated K values. The closeness of the slope of the linear

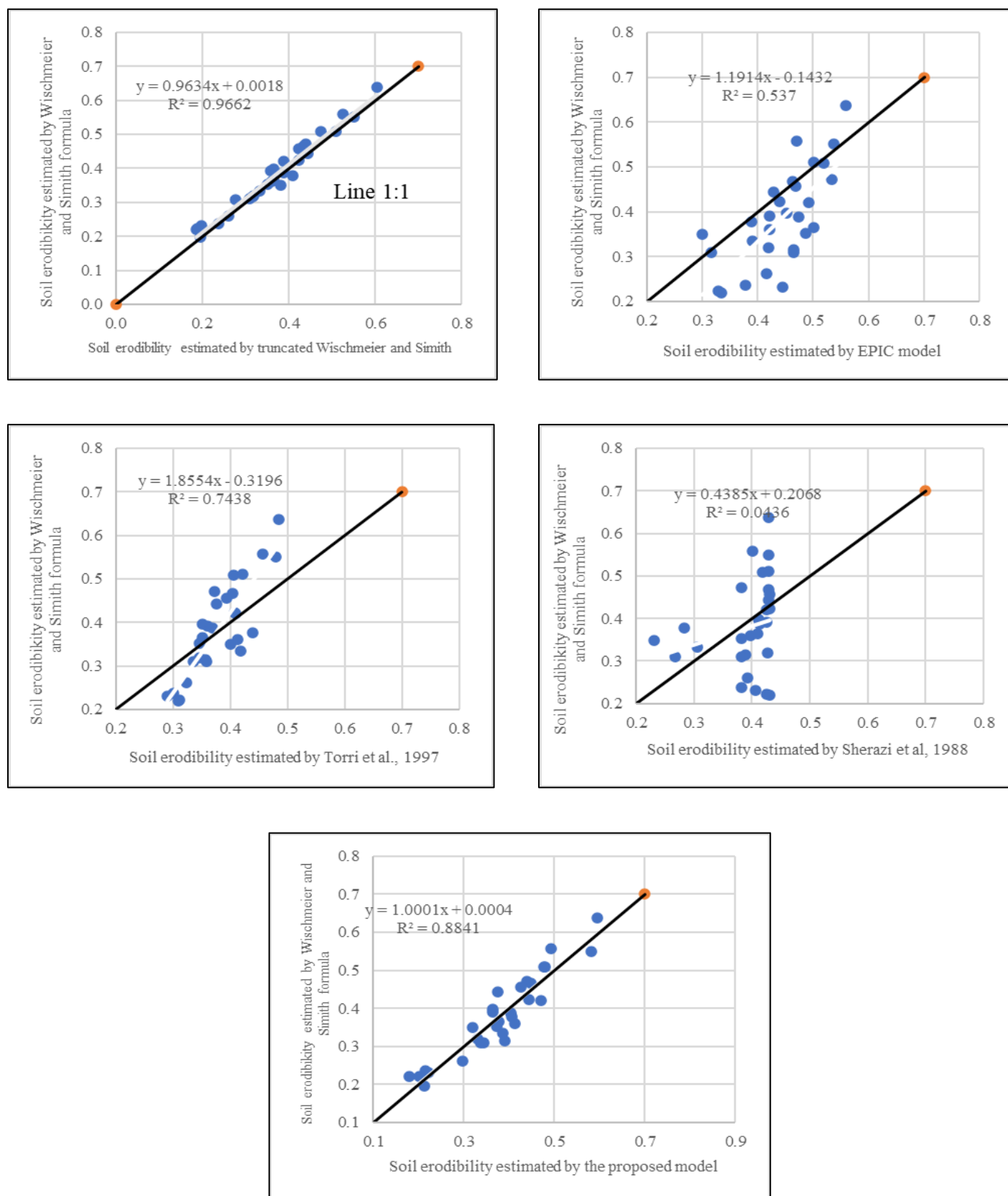
relationship between soil erodibility estimated by the reference method and the estimated value by each of these models to unity is an indication of an acceptable match.

The closeness of the intercept of the linear relation is an additional indication of a good match between observed and predicted values. The high predictability power of the K2 model compared to the remaining models is due to the fact that K2 resembles the K1 model from all aspects except that the permeability term is removed from the K2 model. Furthermore, the permeability code of most of the study soils is 3 or close to 3. This will eliminate the effect of permeability on K prediction. Unlike K2 and K6 models, the remaining models offered poor performance with considerable deviations from the line 1:1.

To further confirm the predictability power of the applied models, a host of performance indicators were determined and presented in Table 8. Judging from mean biased error (MBE) and coefficient of residual mass (CRM), the K6 model neither overestimated nor underestimated the soil erodibility, while K2 and K4 underestimated the K value. In contrast, the K3 and K5 models overestimated the K values. Moreover, the results indicated that the K2 model offered the lowest values for mean absolute error (MAE) and root mean square error (RMSE), and K6 offered the second lowest values for these indicators. It was also observed that the K6 offered the lowest value for the mean absolute percentage error (MAPE = 4.867%), followed by the K2 model (MAPE = 5.133%). The reverse of these results is true for the remaining models. Judging from the coefficient of agreement (d) and Nash-Sutcliffe index, the K2 model also exhibited the highest power of predictability followed by the K6 model. It also presents the results of using multiple performance indicators <sup>[39]</sup>.

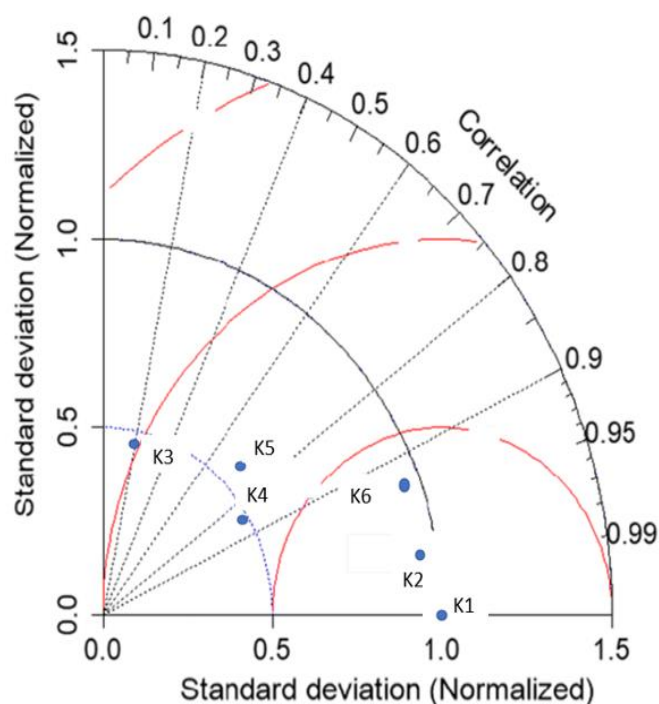
**Table 8:** Some selected performance indicators to test the predictability power of the study models for estimating soil erodibility.

| Performance Indicators | Model                          |                       |                     |            |                |
|------------------------|--------------------------------|-----------------------|---------------------|------------|----------------|
|                        | Truncated Wischmeier and Smith | Shirazi et al. (1988) | Torri et al. (1997) | EPIC model | Proposed model |
| MBE                    | 0.012                          | - 0.014               | 0.003               | - 0.059    | 0.000          |
| MAE                    | 0.017                          | 0.088                 | 0.061               | 0.076      | 0.033          |
| MAPE                   | 5.133                          | 30.384                | 17.520              | 25.428     | 4.867          |
| RMSE                   | 0.023                          | 0.111                 | 0.070               | 0.096      | 0.037          |
| CRM                    | 0.032                          | - 0.040               | 0.007               | - 0.156    | 0.001          |
| CV                     | 6.148                          | 29.240                | 18.420              | 25.161     | 9.735          |
| D                      | 0.988                          | 0.427                 | 0.800               | 0.738      | 0.969          |
| NC                     | 0.994                          | 0.859                 | 0.944               | 0.896      | 0.984          |



**Figure 5:** Plot of estimated soil erodibility by the different models versus the estimated values by Wischmeier and Smith, 1978.

A close evaluation of the applied models was also performed by using the Taylor diagram of Figure 6. The main objective was to show the consistency between the K values estimated by the K1 models and the estimated K values by the remaining models. In this figure, the K1 model was considered as the reference method. Six points were plotted, each representing a model. The coordinates of each point are its normalized standard deviation and its correlation with the reference model. As can be seen in the diagram, K2 is the closest point to the reference point, followed by K6, while the K3 model is the farthest point from the reference point. However, the applied models can be ranked in the following order according to their effectiveness or predictability power. However, the applied models can be ranked in the following order according to their effectiveness or predictability power:  $K2 > K6 > K4 > K5 > K3$ . It seems from the above results that the K2 and K6 models are the best candidates for predicting soil erodibility over the area under study. The advantages of these two models are ease of application and their low cost.



**Figure 6:** Taylor diagram to characterize the relationship between the tested models and the reference model.

### 3.9 Spatial Distribution of Soil Erodibility over the Study Area

After selecting the IDW as the best interpolation method, continuous surfaces were generated in a GIS environment for soil erodibility estimated by the applied models, and the results are displayed in Figure 7. Overall, it is obvious from Figure 7 that the K-factor values are the highest in the south and tend to decrease towards the north of the study area. A decrease in clay content, organic matter, and stable aggregates and an increase in silt

content as one moves from north to south are responsible for such a trend. The results also indicated that drawn maps did not exhibit an obvious pattern for soil erodibility from east to west. It is also evident from Figure 7 that the applied models did not provide a similar spatial distribution. It is commendable to indicate that such type of study is important because it assists the researchers in developing suitable soil conservation measures that can preserve the integrity of the soil through reducing soil erosion and sedimentation <sup>[40,41]</sup>.

## Conclusions

The results of the current study indicated that the majority of the soil erodibility values estimated by the reference method fell in moderate and fairly high classes. It is also apparent from the displayed results that more than two-thirds of the sampling sites have a dispersion ratio of more than 15% indicating that the majority of the soils are highly susceptible to erosion. It can also be concluded from the results that the Truncated Wischmeier and Smith and the proposed models outperformed the Sherazi et al (1988), Torre et al (1997), and the EPIC models. Moreover, the soil erodibility estimated by the reference model has the highest value in the north and tends to decrease as one moves from north to south.

## Authors' contributions

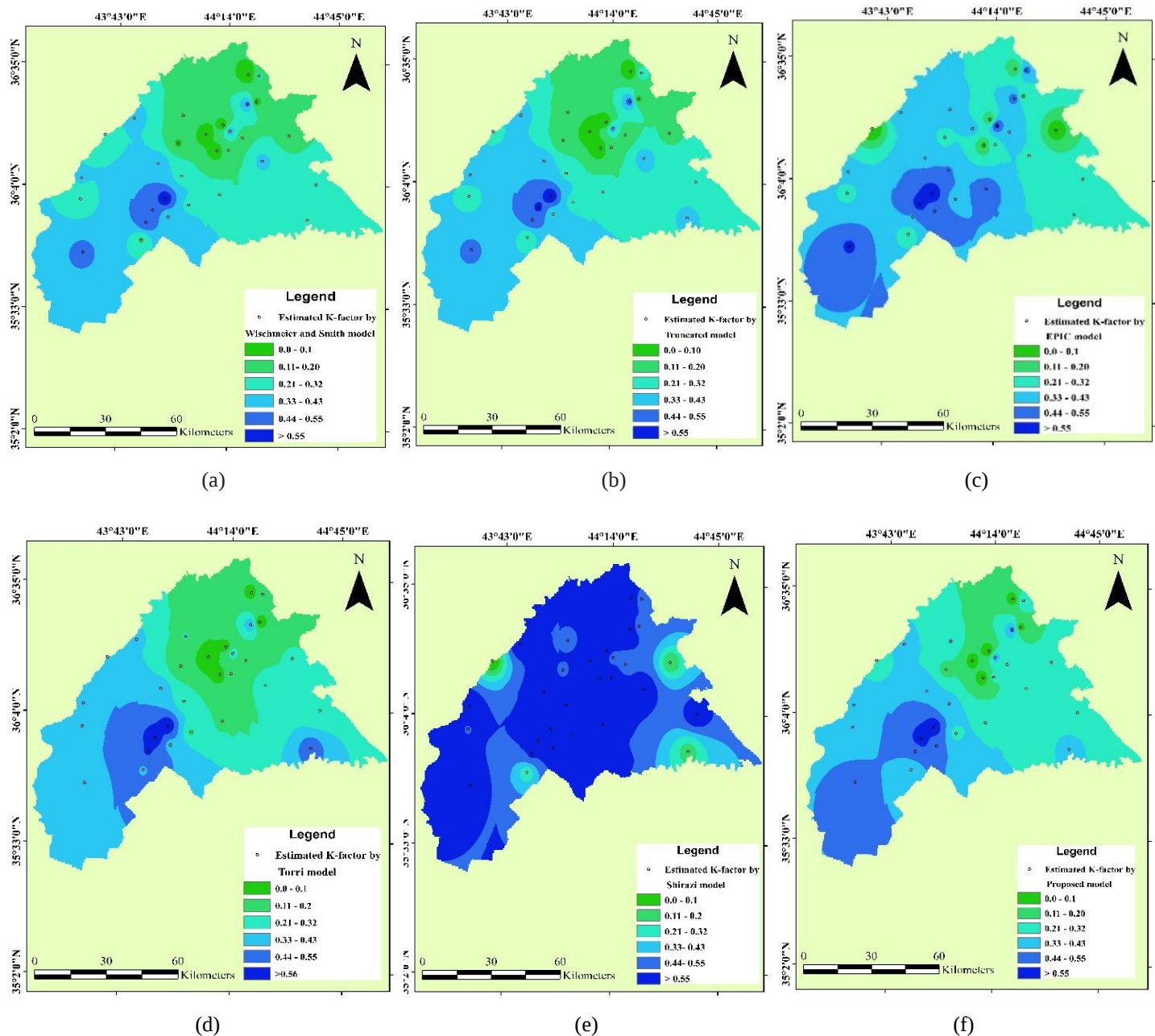
Tariq H. Karim: Supervision, Conceptualization, Methodology, Writing - original draft preparation. Kamyar M. Mohammed: Methodology, Formal analysis and investigation, Writing-review and editing, Resources.

## Competing interests

The authors of this article declare no competing interests.

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**Figure 7 a, b, c, d, e, and f:** Spatial distribution estimated by different models over the study area.

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